

Exercise 01 :

Show by considering $\phi = \phi(t, x, y, z)$ that the material derivative

$$d\phi/dt = \partial\phi/\partial t + \mathbf{v} \cdot \nabla\phi$$

Exercise 02

A calorically imperfect ideal gas is known to have

$$C_P(T) = C_{P0} + aT.$$

A sample of this gas begins at P_1, T_1 . It is heated isobarically to T_2 , and expanded isochorically to T_3 .

Find the change in internal energy of the gas, $u_3 - u_1$

Exercise 03

Consider a pure fluid of one component. Show that

$$\left(\frac{\partial c_V}{\partial v}\right)_T = T \left(\frac{\partial^2 p}{\partial T^2}\right)_v.$$

Exercise 04

From stability arguments, show that the enthalpy of a pure fluid is a convex function of entropy and a concave function of pressure.

$$\left(\frac{\partial^2 h}{\partial s^2}\right)_p = \left(\frac{\partial T}{\partial s}\right)_p = \frac{T}{c_p} > 0.$$

Exercise 05

Determine the total differential of volume for an ideal gas dV